# Pathfinding Algorithms for Mutating Graphs 

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## 1 Abstract

Consider a map of an unknown place represented as a graph, where vertices represent landmarks and edges represent connections between landmarks. You have current information on whether each edge is traversible, as well past data about the availability of each connection. You have a preset destination that you want to reach as fast as possible. Pathfinding algorithms for static graphs involve computing the whole path from start to destination, but if the graph is rapidly changing, say due to some extreme environmental condition, then calculating the whole path in the beginning will not be feasible. The purpose of this project is to design and compare different pathfinding algorithms for a graph whose structure mutates to a significant extent. Algorithms may involve probabilistic theory, dynamic programming, heuristics, genetic programming, and variations of standard shortest-path algorithms such as Dijkstra's algorithm.

## 2 Introduction

The problem statement is as follows: given an initial graph structure of a mutating graph, a start vertex, an end vertex, and an edge history for every pair of vertices, develop an algorithm to travel from the start vertex to the end vertex. The mutating graph will be implemented in timesteps. After each move, each edge will either stay the same or be toggled by some random function of the current state of the graph. The plan is to create a sturdy algorithm for the general case of the problem, as well as variations for specific cases where the main algorithm would not be as effective. Algorithms will be compared and analyzed to determine the circumstances for which each one is best. This project will involve both theory and actual programming.

## 3 Background Literature

There are little to no studies available concerning mutating graphs, so research has been focused on graph theory in general as well as the more specific topic of dynamic graphs, which may change in structure. General shortest path and flow algorithms have been reviewed. Dynamic graph algorithms and query/update algorithms have been reviewed lightly. The results from this project are expected to be completely new and original.

## 4 Theory and Algorithms

Define randomized distance as the distance to destination node taking the possibility of graph mutation into account. For example, a vertex with two unit length paths leading to the destination will be closer in this sense
than a vertex with only one. We use steady-state convergence and methods from numerical analysis to set up a system of equations we want the randomized distances to satisfy, and solve the system. We use dynamic programming to approximate distance to heuristically closer points first, then base calculations for farther vertices on these approximations. We use the previous states of the graph: we can use this data to develop a hashmap to approximate future mutations. The hashmap stores each mutating as a mapping from the original state to the new state, and then calculates the probability of toggling states. Then, that probability is used to calculate the probability that an edge will exist in any number of timesteps. We use genetic programming to find optimal values for algorithm-specific variables, such as probability estimate multipliers and heuristic functions. We focus on sparse graphs, graphs where the number of edges is significantly less than the square of the number of vertices. The edge weights are limited to positive doubles so mutation will be somewhat controlled; edge weights that are too large will never be traversed anyway.

Currently, the algorithm proceeds chronologically, then for each vertex, it calculates the optimal vertex in the previous time step that could have led to this vertex. It uses the history hash map to predict the graph structure at that timestep, and uses an approximation error to weight lower timesteps. Then, it backtracks to find the best vertex after the first timestep to visit. This is the main body of the working java implementation of this algorithm:

```
for(int v=0; v<vertices; v++) prevvals[v] = inf;
prevvals[curvertex] = 0;
for(int t=0; t<tlimit; t++)
{
for(int v=0; v<vertices; v++)
{
curvals[v] = inf;
for(int e=0; e<adjlist[v].size(); e++)
{
Edge E = (Edge)adjlist[v].get(e);
if(prevvals[E.getVertex(v)]>=inf) continue;
double x = globhist.predictMutations(E.getWeight(),t) + prevvals[E.getVertex(v)
if(x<curvals[v])
{
curvals[v] = x;
bestprev[v][t] = E;
}
}
}
for(int v=0; v<vertices; v++)
prevvals[v] = curvals[v];
if(curvals[vend]<inf)
```

```
{
if(curvals[vend]<bestend||estend<0)
{
bestendtime = t;
bestend = curvals[vend];
}
}
else if(t==tlimit-1) System.out.println("Time limit is insufficient for the wid
}
int btrack = vend;
for(int t=bestendtime; t>0; t--)
{
System.out.println(t + " " + btrack);
btrack = bestprev[btrack][t].getVertex(btrack);
}
return bestprev[btrack] [0];
```


## 5 Testing

The testing interface as well as the algorithms themselves will be written in Java. Since graphs are difficult to develop graphics for, output will be limited to textual lists and charts. Testing will be done by generating graph structures and initial weights and devising a system for the random edge weight mutation. Then, repeated simulations will be run and the algorithms will be scored based on their performance for various types of starting parameters.

First, the algorithms will be tested for functionality and stability by examining its pathfinding in the interface and seeing if it behaves as expected. Then, algorithms will be tested for efficiency through random and user-specified initial states. Algorithms will be compared based on how fast they can find their destination, runtime complexity, and memory usage. If the algorithms take parameters, then genetic algorithms can be used to find optimal values for the parameters.

Second quarter was devoted solely to building algorithms and developing theory for solving the problem. Testing and variating will begin third quarter. The results should be ready by the end of third quarter and fourth quarter will be focused on analyzing and finishing off the project and writing it up.

## 6 Expected Results

Results will consist of the efficiency, complexity, and stability of the algorithms tested. Results will be presented in charts, data tables, qualitative statements, and possibly graphics. Applications of the results are undetermined as this point, since this is not a commonly trod subfield of graph
theory. Robots may be able to apply the algorithms in natural or manmodeled environments. The graph may be able to simulate a transportation network in order to find paths for pioneers. The randomly mutating edge weights may represent an unknown cause of change in an environment, even if there is a systematic pattern to the change. The factor may simply be too complex to model exactly and would be better approximated by a random variable. The project may be useful for applications further into the future, or may spark further development in the area which will lead to results that may be put into practice.

## 7 Literature Cited

## References

[1] D. Frigoni, M. Ioffreda, U. Nanni, G. Pasqualbne, "Experimental Analysis of Dynamic Algorithms for the Single Source Shortest Paths Problem", 2000. http://www.acm.org/jea/TURING/Vol3Nbr5.pdf.

